立命館大学幾何学セミナー

来る**8月29日(金)**に立命館大学幾何学セミナーが行われます. みなさまのご参加をお待ちいたしております.

日時: 2025年8月29日(金) 16:30~17:30

開催方法: ハイブリッド開催(立命館大学びわこ・くさつキャンパス ウェストウィング 6 階談話会室での対面開催及び Zoom ミーティングによる配信)を予定. Zoom 参加の場合,下記の URL よりご登録ください. ご登録いただいた電子メールアドレスへ, Zoom ミーティングの URL 等をお知らせいたします.

https://ritsumei-ac-jp.zoom.us/meeting/register/KB-80qipSnKhzhIcPoto9Q

講演者:

Wolfram BAUER 氏

(Leibniz Universität Hannover)

タイトル:

Global lifting and fundamental solution of degenerate operators

アブストラクト:

This talk applies and extends topics of the special lecture course "Subriemannian Geometry and Analysis" which was held at Ritsumeikan University during this week.

On \mathbb{R}^n we consider Hörmander operators \mathcal{L} that are homogeneous of degree 2 with respect to a non-isotropic dilation. Based on a global lifting-procedure by G.B. Folland in [2] there is a Carnot Lie group \mathbb{G} such that \mathcal{L} lifts through a polynomial surjective map $\pi: \mathbb{G} \to \mathbb{R}^n$ to a sub-Laplacian $\mathcal{L}_{\mathbb{G}}$ in sub-Riemannian geometry on \mathbb{G} . Due to the additional group and dilation structure existence and properties of a global fundamental solution to \mathcal{L} can be descended through π from corresponding known properties of a fundamental solution to $\mathcal{L}_{\mathbb{G}}$. This lifting and descending process can be made explicit and by choosing suitable coordinates useful estimates or even explicit formulas can be obtained. Partly this talk is based on [1] by S. Biagi and A. Bonfiglioli (2017).

References:

- [1] S. Biagi, A. Bonfiglioli, The existence of a global fundamental solution for homogeneous Hörmander operators via a global lifting method, Proc. London Math. Soc. (3), 114 (2017), 855-889.
- [2] G.B. Folland, On the Rothschild-Stein lifting theorem, Comm. Partial Differential Equations 2, 161 207, (1977).

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